



Introduction

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2021-11-03





Course Information

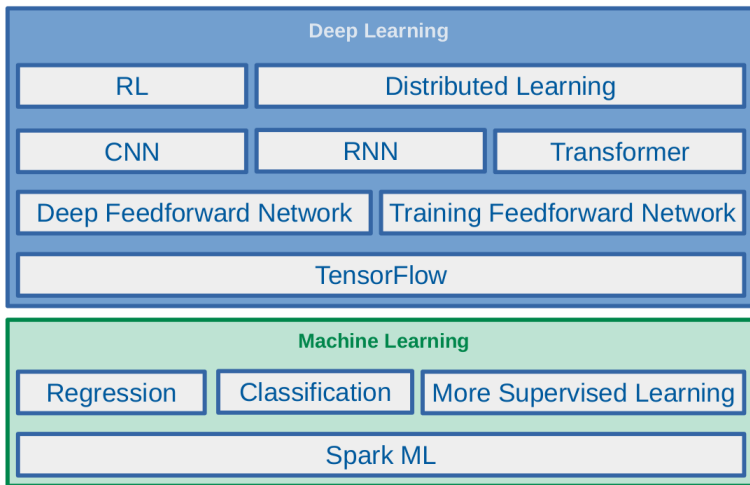


Course Objective

- ▶ This course has a **system-based** focus.
- ▶ Learn the **theory** of **machine learning and deep learning**.
- ▶ Learn the **practical aspects** of building **machine learning and deep learning** algorithms using data **parallel programming platforms**, such as **Spark and TensorFlow**.



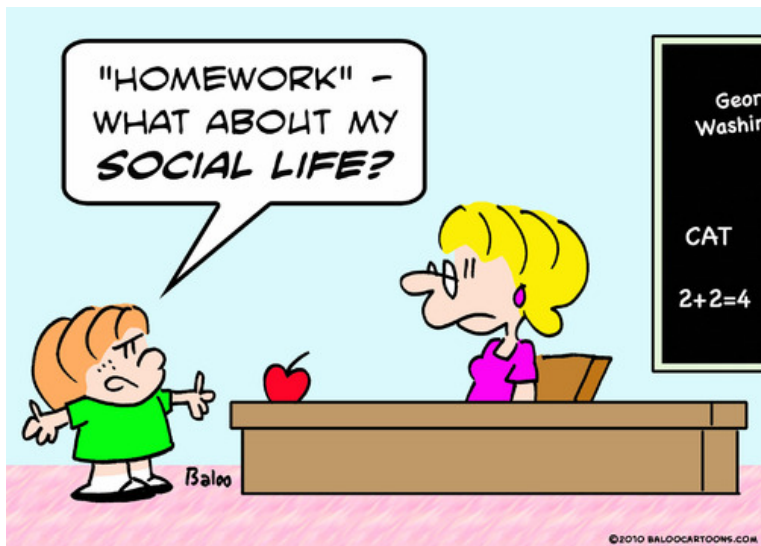
Topics of Study





Intended Learning Outcomes (ILOs)

- ▶ **ILO1:** explain the **principles** of **ML/DL algorithms** and apply their techniques to solve problems.
- ▶ **ILO2:** explain different **DNN architectures**, such as CNN, RNN, etc., and know how to build and train such networks.
- ▶ **ILO3:** explain the **principles** of **distributed learning**.
- ▶ **ILO4:** implement **ML/DL algorithms** using **Spark** and **TensorFlow**.





The Course Assessment

- ▶ **Task1**: the **review** questions (P/F)
- ▶ **Task2**: the **lab** assignments (A-F)
- ▶ **Task3**: the final **project** (A-F)



How Each ILO is Assessed?

	Task1	Task2	Task3
ILO1	x		
ILO2	x		
ILO3	x		
ILO4	x	x	x



Task1: The Review Questions (A-F)

- ▶ One review question **per week**.
- ▶ Questions about the **lectures**.
- ▶ The review questions are **graded (A-F)**.



Task2: The Lab Assignments (A-F)

- ▶ Two lab assignments: **source code** and **oral presentation**.
- ▶ E: source code
- ▶ D: source code + half questions (basic)
- ▶ C: source code + all questions (basic)
- ▶ B: source code + half questions (basic and advanced)
- ▶ A: source code + all questions (basic and advanced)



Task3: The Final Project (A-F)

- ▶ One final project: **source code** and **oral presentation**.
- ▶ **Proposed by students** and confirmed by the teacher: **A-level** or **C-level** proposals.
- ▶ **E**: C-level source code
- ▶ **D**: C-level source code + half questions (basic and advanced)
- ▶ **C**: C-level source code + all questions (basic and advanced) or A-level source code + all questions (basic)
- ▶ **B**: A-level source code + half questions (basic and advanced)
- ▶ **A**: A-level source code + all questions (basic and advanced)



The Final Grade

- ▶ The **final grade** is the **weighted average** of the **review questions** (0.2), **two labs** (0.25 each), and the **final project** (0.3).
- ▶ To compute it, map **A-E to 5-1**, and take the average.
- ▶ The floating values are **rounded up**, if they are **more than half**, otherwise they are **rounded down**.
 - E.g., **3.6** will be rounded to **4**, and **4.5** will be rounded to **4**.
- ▶ A **late** submission will **reduce you grade level by one**. That is, A will become B, B will become C, and so on.
- ▶ To pass the course, you need to take **at least E** in **all the assignments**.

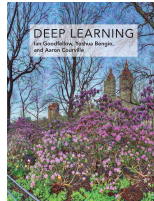
How to Submit the Assignments?

- ▶ Through the [Canvas](#) site.
- ▶ Students will work in **groups of two** on all the [Tasks 1-4](#).



The Course Material

- ▶ **Hands-on machine learning with Scikit-Learn and TensorFlow, 2nd Edition**, A. Geron, O'Reilly Media, 2019
- ▶ **Deep learning**, I. Goodfellow et al., Cambridge: MIT press, 2016
- ▶ **Spark - The Definitive Guide**, M. Zaharia et al., O'Reilly Media, 2018.





The Course Web Page

`https://id2223kth.github.io`



The Questions-Answers Page

<https://tinyurl.com/6s5jy46a>



The Course Overview

Sheepdog or Mop



Chihuahua or Muffin



Barn Owl or Apple





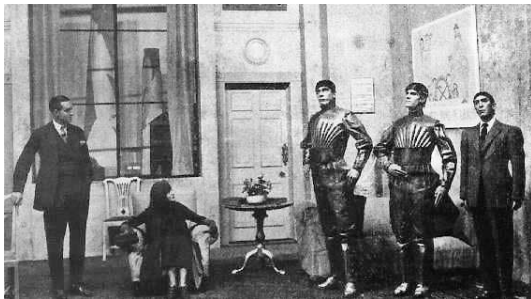
Artificial Intelligence Challenge

- ▶ **Artificial intelligence (AI)** can solve problems that can be described by a **list of formal mathematical rules**.
- ▶ The **challenge** is to solve the tasks that are **hard for people to describe formally**.
- ▶ Let computers to **learn** from **experience**.

History of AI

1920: Rossum's Universal Robots (R.U.R.)

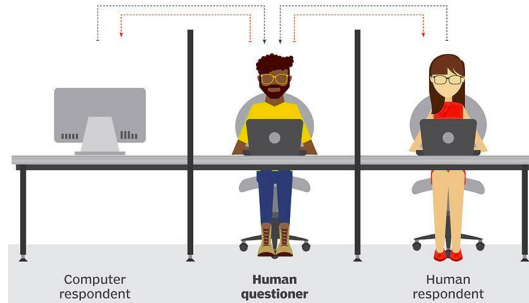
- ▶ A science fiction play by Karel Čapek, in 1920.
- ▶ A factory that creates artificial people named robots.



[<https://dev.to/lshultebraucks/a-short-history-of-artificial-intelligence-7hm>]

1950: Turing Test

- ▶ In 1950, **Turing** introduced the **Turing test**.
- ▶ An attempt to define **machine intelligence**.



[<https://searchenterpriseai.techtarget.com/definition/Turing-test>]

1956: The Dartmouth Workshop

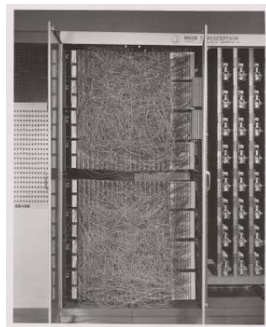
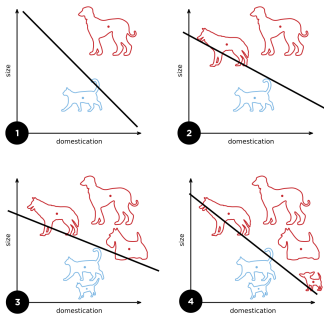
- ▶ Probably the first workshop of AI.
- ▶ Researchers from CMU, MIT, IBM met together and founded the AI research.



[<https://twitter.com/lordsaicom/status/898139880441696257>]

1958: Perceptron

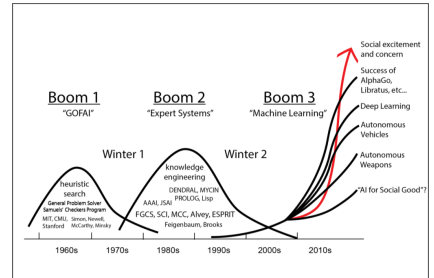
- ▶ A supervised learning algorithm for binary classifiers.
- ▶ Implemented in custom-built hardware as the Mark 1 perceptron.



[<https://en.wikipedia.org/wiki/Perceptron>]

1974–1980: The First AI Winter

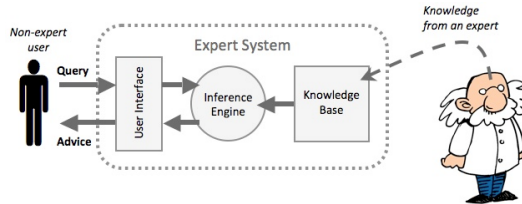
- ▶ The over **optimistic settings**, which were not occurred
- ▶ The **problems**:
 - Limited **computer power**
 - Lack of **data**
 - Intractability and the **combinatorial explosion**



[<http://www.technologystories.org/ai-evolution>]

1980's: Expert systems

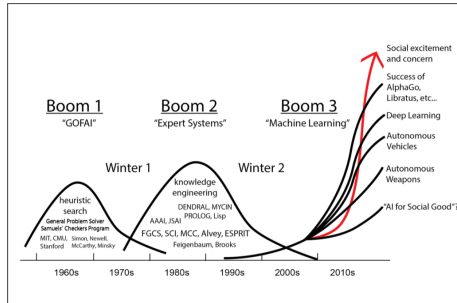
- ▶ The programs that solve problems in a **specific domain**.
- ▶ **Two** engines:
 - **Knowledge engine**: **represents** the **facts and rules** about a specific topic.
 - **Inference engine**: **applies** the **facts and rules** from the knowledge engine to new facts.



[https://www.igcseict.info/theory/7_2/expert]

1987–1993: The Second AI Winter

- ▶ After a series of **financial setbacks**.
- ▶ The fall of **expert systems** and **hardware companies**.



[<http://www.technologystories.org/ai-evolution>]

1997: IBM Deep Blue

- ▶ The first chess computer to beat a world chess champion Garry Kasparov.



[<http://marksist.org/icerik/Tarihte-Bugun/1757/11-Mayis-1997-Deep-Blue-adli-bilgisayar>]



2012: AlexNet - Image Recognition

- ▶ The ImageNet competition in image classification.
- ▶ The AlexNet Convolutional Neural Network (CNN) won the challenge by a large margin.

IMGENET

2016: DeepMind AlphaGo

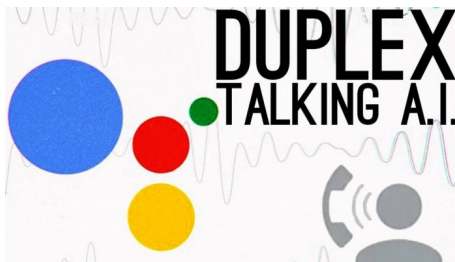
- ▶ DeepMind AlphaGo won Lee Sedol, one of the best players at Go.
- ▶ In 2017, DeepMind published AlphaGo Zero.
 - The next generation of AlphaGo.
 - It learned Go by playing against itself.



[<https://www.zdnet.com/article/google-alphago-caps-victory-by-winning-final-historic-go-match>]

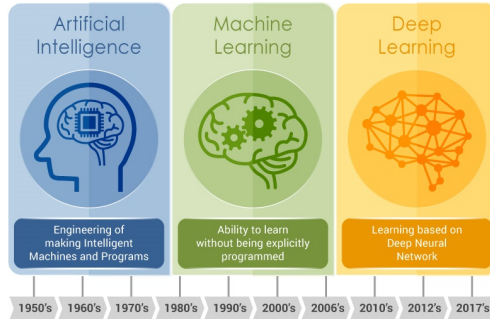
2018: Google Duplex

- ▶ An AI system for accomplishing **real-world tasks over the phone**.
- ▶ A **Recurrent Neural Network (RNN)** built using **TensorFlow**.



AI Generations

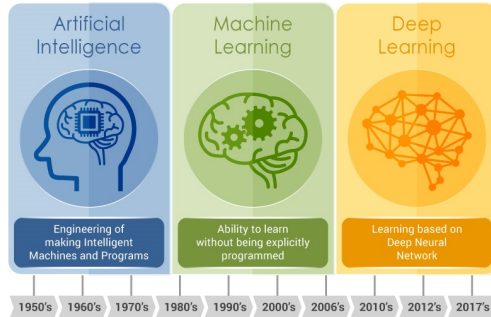
- ▶ Rule-based AI
- ▶ Machine learning
- ▶ Deep learning



[<https://bit.ly/2woLEzs>]

AI Generations - Rule-based AI

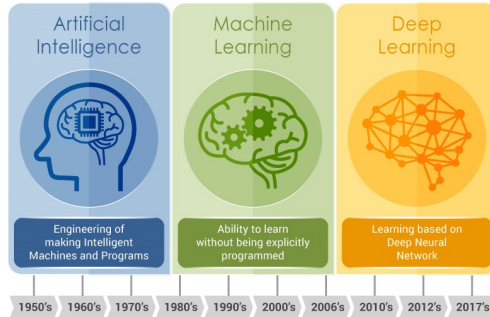
- ▶ **Hard-code** knowledge
- ▶ Computers reason using **logical inference rules**



[<https://bit.ly/2woLEzs>]

AI Generations - Machine Learning

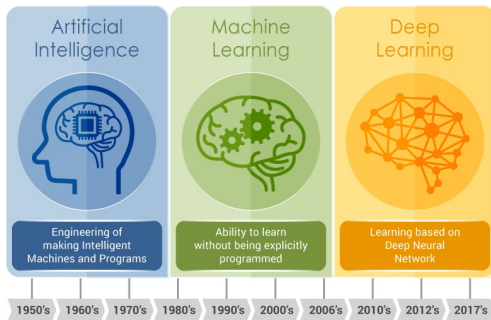
- ▶ If AI systems acquire **their own knowledge**
- ▶ **Learn from data** without being explicitly programmed



[<https://bit.ly/2woLEzs>]

AI Generations - Deep Learning

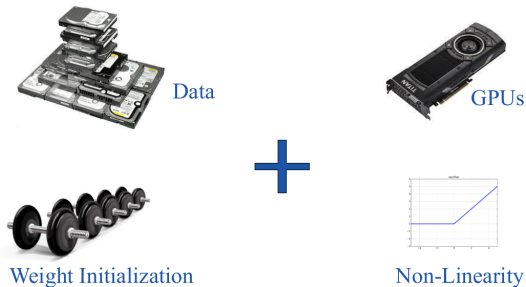
- ▶ For many tasks, it is **difficult to know what features** should be extracted
- ▶ Use **machine learning** to **discover** the mapping from **representation to output**



[<https://bit.ly/2woLEzs>]

Why Does Deep Learning Work Now?

- ▶ Huge quantity of data
- ▶ Tremendous increase in computing power
- ▶ Better training algorithms





Machine Learning and Deep Learning

Learning Algorithms

- ▶ A **ML algorithm** is an algorithm that is able to **learn from data**.
- ▶ What is **learning**?
- ▶ A computer program is said to **learn** from **experience E** with respect to some class of **tasks T** and **performance measure P**, if its performance at tasks in **T**, as measured by **P**, improves with experience **E**. (Tom M. Mitchell)



Learning Algorithms - Example 1

- ▶ A **spam filter** that can learn to flag **spam** given examples of **spam emails** and examples of **regular emails**.
- ▶ **Task T**: flag spam for new emails
- ▶ **Experience E**: the training data
- ▶ **Performance measure P**: the ratio of correctly classified emails



[<https://bit.ly/2oip1YM>]

Learning Algorithms - Example 2

- ▶ Given dataset of prices of 500 houses, how can we learn to **predict the prices** of other houses, as a **function of the size of their living areas**?
- ▶ **Task T**: predict the price
- ▶ **Experience E**: the dataset of living areas and prices
- ▶ **Performance measure P**: the difference between the predicted price and the real price

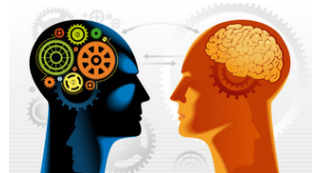


[<https://bit.ly/2MyiJUy>]

Types of Machine Learning Algorithms

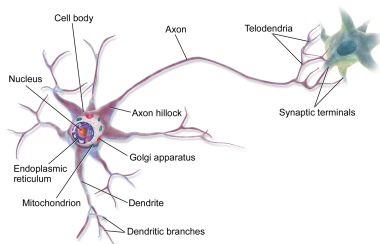
- ▶ **Supervised learning**
 - Input data is **labeled**, e.g., spam/not-spam or a stock price at a time.
 - **Regression vs. classification**

- ▶ **Unsupervised learning**
 - Input data is **unlabeled**.
 - Find **hidden structures** in data.



From Machine Learning to Deep Learning

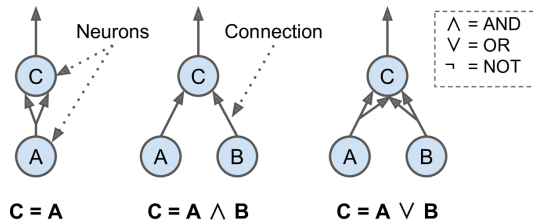
- ▶ **Deep Learning (DL)** is part of **ML** methods based on learning **data representations**.
- ▶ Mimic the **neural networks of our brain**.



[A. Geron, O'Reilly Media, 2017]

Artificial Neural Networks

- ▶ **Artificial Neural Network (ANN)** is inspired by **biological neurons**.
- ▶ **One or more binary inputs** and **one binary output**
- ▶ **Activates its output** when more than a **certain number of its inputs** are active.



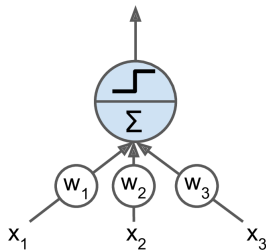
[A. Geron, O'Reilly Media, 2017]

The Linear Threshold Unit (LTU)

- ▶ Inputs of a LTU are **numbers** (not binary).
- ▶ Each **input connection** is associated with a **weight**.
- ▶ Computes a **weighted sum of its inputs** and applies a **step function** to that **sum**.

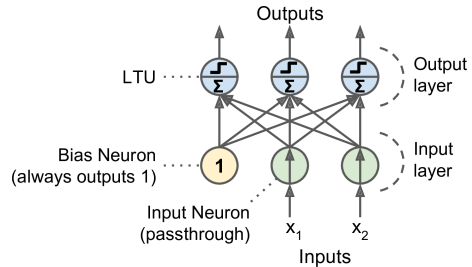
- ▶ $z = w_1x_1 + w_2x_2 + \dots + w_nx_n = w^T x$

- ▶ $\hat{y} = \text{step}(z) = \text{step}(w^T x)$



The Perceptron

- ▶ The **perceptron** is a **single layer of LTUs**.
- ▶ The **input neurons** output whatever **input they are fed**.
- ▶ A **bias neuron**, which just **outputs 1 all the time**.



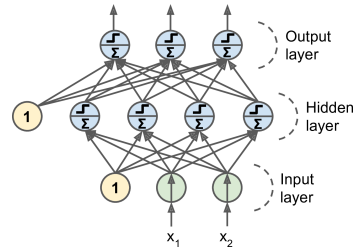


Deep Learning Models

- ▶ Deep Neural Network (**DNN**)
- ▶ Convolutional Neural Network (**CNN**)
- ▶ Recurrent Neural Network (**RNN**)
- ▶ Transformer
- ▶ Deep Reinforcement Learning

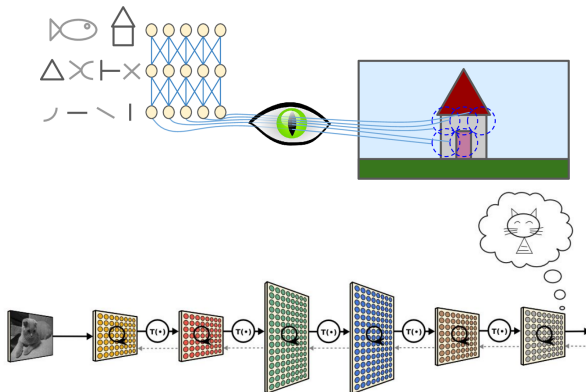
Deep Neural Networks

- ▶ Multi-Layer Perceptron (MLP)
 - One **input layer**.
 - One or more layers of **LTUs** (hidden layers).
 - One **final layer of LTUs** (output layer).
- ▶ Deep Neural Network (DNN) is an ANN with **two or more hidden layers**.
- ▶ **Backpropagation** training algorithm.



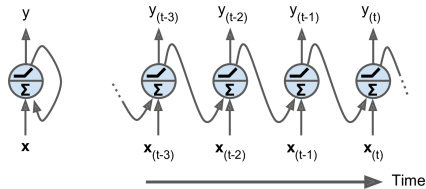
Convolutional Neural Networks

- ▶ Many neurons in the **visual cortex** react only to a **limited region** of the visual field.
- ▶ The **higher-level** neurons are based on the outputs of **neighboring lower-level** neurons.



Recurrent Neural Networks

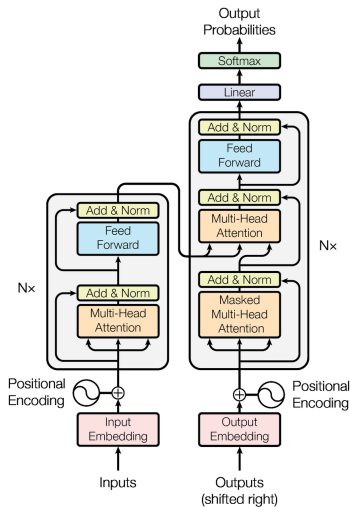
- ▶ The **output** depends on the **input** and the **previous computations**.



- ▶ Analyze **time series data**, e.g., stock market, and autonomous driving systems.
- ▶ Work on sequences of **arbitrary lengths**, rather than on **fixed-sized inputs**.



Transformer



[A. Vaswani et al., Attention Is All You Need, 2017]



Linear Algebra Review



Vector

- ▶ A **vector** is an array of numbers.
- ▶ Notation:
 - Denoted by **bold lowercase letters**, e.g., \mathbf{x} .
 - \mathbf{x}_i denotes the i th entry.

$$\mathbf{x} = \begin{bmatrix} x_1 \\ x_2 \\ \vdots \\ x_n \end{bmatrix}$$



Matrix and Tensor

- ▶ A **matrix** is a 2-D array of numbers.
- ▶ A **tensor** is an array with more than two axes.
- ▶ **Notation:**
 - Denoted by **bold uppercase letters**, e.g., A .
 - a_{ij} denotes the entry in i th row and j th column.
 - If A is $m \times n$, it has m rows and n columns.

$$A = \begin{bmatrix} a_{1,1} & a_{1,2} & a_{1,3} & \dots & a_{1,n} \\ a_{2,1} & a_{2,2} & a_{2,3} & \dots & a_{2,n} \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ a_{m,1} & a_{m,2} & a_{m,3} & \dots & a_{m,n} \end{bmatrix}$$



Matrix Addition and Subtraction

- ▶ The **matrices** must have the same dimensions.

$$A = \begin{bmatrix} a & b \\ c & d \end{bmatrix} + \begin{bmatrix} e & f \\ g & h \end{bmatrix} = \begin{bmatrix} a + e & b + f \\ c + g & d + h \end{bmatrix}$$

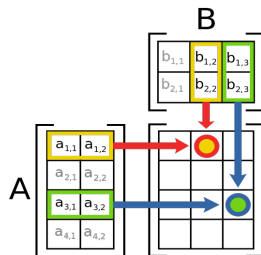
Matrix Product

- ▶ The **matrix product** of matrices **A** and **B** is a third matrix **C**, where $C = AB$.
- ▶ If **A** is of shape $m \times n$ and **B** is of shape $n \times p$, then **C** is of shape $m \times p$.

$$c_{ij} = \sum_k a_{ik} b_{kj}$$

- ▶ Properties

- Associative: $(AB)C = A(BC)$
- Not commutative: $AB \neq BA$



[https://en.wikipedia.org/wiki/Matrix_multiplication]



Matrix Transpose

- ▶ Swap the **rows and columns** of a matrix.

$$A = \begin{bmatrix} a & b \\ c & d \\ e & f \end{bmatrix} \Rightarrow A^T = \begin{bmatrix} a & c & e \\ b & d & f \end{bmatrix}$$

- ▶ Properties

- $A_{ij} = A_{ji}^T$
- If A is $m \times n$, then A^T is $n \times m$
- $(A + B)^T = A^T + B^T$
- $(AB)^T = B^T A^T$



Inverse of a Matrix

- ▶ If A is a **square** matrix, its **inverse** is called A^{-1} .

$$AA^{-1} = A^{-1}A = I$$

- ▶ Where I , the **identity** matrix, is a **diagonal matrix** with all **1's on the diagonal**.

$$I_2 = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \quad I_3 = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$



L^p Norm for Vectors

- ▶ We can measure the **size of vectors** using a **norm** function.
- ▶ Norms are functions **mapping vectors to non-negative values**.

- ▶ L^1 norm

$$\|x\|_1 = \sum_i |x_i|$$

- ▶ L^2 norm

$$\|x\|_2 = \left(\sum_i |x_i|^2 \right)^{\frac{1}{2}} = \sqrt{x_1^2 + x_2^2 + \dots + x_n^2}$$

- ▶ L^p norm

$$\|x\|_p = \left(\sum_i |x_i|^p \right)^{\frac{1}{p}}$$



Probability Review



Random Variables

- ▶ **Random variable:** a **variable** that can take on **different values** randomly.
- ▶ Random variables may be **discrete** or **continuous**.
 - **Discrete** random variable: **finite or countably infinite** number of states
 - **Continuous** random variable: **real value**
- ▶ **Notation:**
 - Denoted by an **upper case letter**, e.g., X
 - Values of a random variable X are denoted by **lower case letters**, e.g., x and y .



Probability Distributions

- ▶ **Probability distribution:** how likely a random variable is to take on each of its possible states.
 - E.g., the random variable X denotes the outcome of a coin toss.
 - The probability distribution of X would take the value 0.5 for $X = \text{head}$, and 0.5 for $Y = \text{tail}$ (assuming the coin is fair).
- ▶ The way we describe probability distributions depends on whether the variables are discrete or continuous.



Discrete Variables

- ▶ **Probability mass function (PMF)**: the probability distribution of a discrete random variable X .
- ▶ **Notation**: denoted by a lowercase p .
 - E.g., $p(x) = 1$ indicates that $X = x$ is certain
 - E.g., $p(x) = 0$ indicates that $X = x$ is impossible
- ▶ **Properties**:
 - The domain D of p must be the set of all possible states of X
 - $\forall x \in D(X), 0 \leq p(x) \leq 1$
 - $\sum_{x \in D(X)} p(x) = 1$



Independence

- ▶ Two random variables X and Y are **independent**, if their **probability distribution** can be expressed as their **products**.

$$\forall x \in D(X), y \in D(Y), p(X = x, Y = y) = p(X = x)p(Y = y)$$

- ▶ E.g., if a **coin is tossed** and a single **6-sided die is rolled**, then the probability of landing on the **head** side of the coin and **rolling a 3** on the die is:

$$p(X = \text{head}, Y = 3) = p(X = \text{head})p(Y = 3) = \frac{1}{2} \times \frac{1}{6} = \frac{1}{12}$$



Conditional Probability

- ▶ **Conditional probability:** the probability of an event given that another event has occurred.

$$p(Y = y \mid X = x) = \frac{p(Y = y, X = x)}{p(X = x)}$$

- ▶ E.g., if 60% of the class passed both labs and 80% of the class passed the first labs, then what percent of those who passed the first lab also passed the second lab?
 - E.g., X and Y random variables for the first and the second labs, respectively.

$$p(Y = \text{lab2} \mid X = \text{lab1}) = \frac{p(Y = \text{lab2}, X = \text{lab1})}{p(X = \text{lab1})} = \frac{0.6}{0.8} = \frac{3}{4}$$



Expectation

- ▶ The **expected value** of a random variable X with respect to a probability distribution $p(X)$ is the **average** value that X takes on when it is drawn from $p(X)$.

$$E_{x \sim p}[X] = \sum_x p(x)x$$

- ▶ E.g., If $X : \{1, 2, 3\}$, and $p(X = 1) = 0.3$, $p(X = 2) = 0.5$, $p(X = 3) = 0.2$
 - $E[X] = 0.3 \times 1 + 0.5 \times 2 + 0.2 \times 3 = 1.9$

Variance and Standard Deviation

- ▶ The **variance** gives a measure of how much the **values of a random variable X** vary as we sample it from its **probability distribution $p(X)$** .

$$\text{Var}(X) = E[(X - E[X])^2]$$
$$\text{Var}(X) = \sum_x p(x)(x - E[X])^2$$

- ▶ E.g., If $X : \{1, 2, 3\}$, and $p(X = 1) = 0.3$, $p(X = 2) = 0.5$, $p(X = 3) = 0.2$
 - $E[X] = 0.3 \times 1 + 0.5 \times 2 + 0.2 \times 3 = 1.9$
 - $\text{Var}(X) = 0.3(1 - 1.9)^2 + 0.5(2 - 1.9)^2 + 0.2(3 - 1.9)^2 = 0.49$
- ▶ The **standard deviation**, shown by σ , is the **square root of the variance**.



Covariance (1/2)

- ▶ The **covariance** gives some sense of **how much two values are linearly related** to each other.

$$\begin{aligned}\text{Cov}(X, Y) &= E[(X - E[X])(Y - E[Y])] \\ \text{Cov}(X, Y) &= \sum_{(x,y)} p(x, y)(x - E[X])(y - E[Y])\end{aligned}$$

Covariance (2/2)

			Y		
	p(X, Y)	1	2	3	p(X)
	1	1/4	1/4	0	1/2
X	2	0	1/4	1/4	1/2
	p(Y)	1/4	1/2	1/4	1

$$E[X] = \frac{1}{2} \times 1 + \frac{1}{2} \times 2 = \frac{3}{2} \quad E[Y] = \frac{1}{4} \times 1 + \frac{1}{2} \times 2 + \frac{1}{4} \times 3 = 2$$

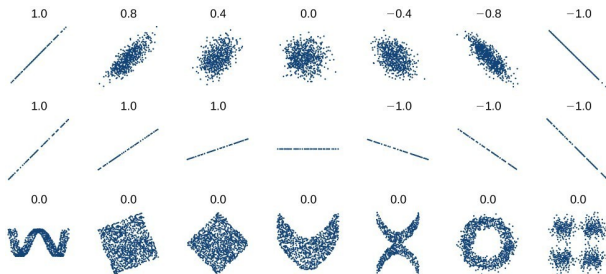
$$\text{Cov}(X, Y) = \sum_{(x,y)} p(x, y)(x - E[X])(y - E[Y])$$

$$= \frac{1}{4}(1 - \frac{3}{2})(1 - 2) + \frac{1}{4}(1 - \frac{3}{2})(2 - 2) + 0(1 - \frac{3}{2})(3 - 2) \\ + 0(2 - \frac{3}{2})(1 - 2) + \frac{1}{4}(2 - \frac{3}{2})(2 - 2) + \frac{1}{4}(2 - \frac{3}{2})(3 - 2) = \frac{1}{4}$$

Correlation Coefficient

- ▶ The **Correlation coefficient** is a quantity that measures the **strength** of the **association** (or **dependence**) between two random variables, e.g., **X** and **Y**.

$$\rho(X, Y) = \frac{\text{Cov}(X, Y)}{\sigma(X)\sigma(Y)}$$





Probability and Likelihood (1/2)

- ▶ Let $X : \{x^{(1)}, x^{(2)}, \dots, x^{(m)}\}$ be a **discrete random variable** drawn **independently** from a **distribution probability p** depending on a **parameter θ** .
 - For six tosses of a coin, $X : \{h, t, t, t, h, t\}$, **h**: head, and **t**: tail.
 - Suppose you have a **coin** with probability θ to land heads and $(1 - \theta)$ to land tails.
- ▶ $p(X | \theta = \frac{2}{3})$ is the **probability** of X given $\theta = \frac{2}{3}$.
- ▶ $p(X = h | \theta)$ is the **likelihood** of θ given $X = h$.
- ▶ **Likelihood (L)**: a function of the **parameters (θ)** of a probability model, given **specific observed data**, e.g., $X = h$.

$$L(\theta | X) = p(X | \theta)$$



Probability and Likelihood (2/2)

- ▶ The **likelihood** differs from that of a **probability**.
- ▶ A **probability** $p(X | \theta)$ refers to the occurrence of **future events**.
- ▶ A **likelihood** $L(\theta | X)$ refers to **past events** with known outcomes.

Maximum Likelihood Estimator

- ▶ If samples in \mathbf{X} are **independent** we have:

$$\begin{aligned}L(\theta | \mathbf{X}) &= p(\mathbf{X} | \theta) = p(\mathbf{x}^{(1)}, \mathbf{x}^{(2)}, \dots, \mathbf{x}^{(m)} | \theta) \\ &= p(\mathbf{x}^{(1)} | \theta)p(\mathbf{x}^{(2)} | \theta) \cdots p(\mathbf{x}^{(m)} | \theta) = \prod_{i=1}^m p(\mathbf{x}^{(i)} | \theta)\end{aligned}$$

- ▶ The **maximum likelihood estimator (MLE)**: what is the **most likely value** of θ given the training set?

$$\hat{\theta}_{\text{MLE}} = \arg \max_{\theta} L(\theta | \mathbf{X}) = \arg \max_{\theta} \prod_{i=1}^m p(\mathbf{x}^{(i)} | \theta)$$

Maximum Likelihood Estimator - Example

- ▶ Six tosses of a coin, with the following model:
 - Possible outcomes: **h** with probability of θ , and **t** with probability $(1 - \theta)$.
 - Results of coin tosses are independent of one another.
- ▶ Data: $X : \{\mathbf{h}, \mathbf{t}, \mathbf{t}, \mathbf{t}, \mathbf{h}, \mathbf{t}\}$

- ▶ The likelihood is

$$\begin{aligned}L(\theta | X) &= p(X | \theta) \\&= p(X = \mathbf{h} | \theta)p(X = \mathbf{t} | \theta)p(X = \mathbf{t} | \theta)p(X = \mathbf{t} | \theta)p(X = \mathbf{h} | \theta)p(X = \mathbf{t} | \theta) \\&= \theta(1 - \theta)(1 - \theta)(1 - \theta)\theta(1 - \theta) \\&= \theta^2(1 - \theta)^4\end{aligned}$$

- ▶ $\hat{\theta}$ is the value of θ that maximizes the likelihood:

$$\hat{\theta}_{\text{MLE}} = \arg \max_{\theta} L(\theta | X) = \frac{2}{2 + 4}$$



Log-Likelihood

- ▶ The MLE product is prone to numerical underflow.

$$\hat{\theta}_{\text{MLE}} = \arg \max_{\theta} L(\theta | X) = \arg \max_{\theta} \prod_{i=1}^m p(x^{(i)} | \theta)$$

- ▶ To overcome this problem we can use the logarithm of the likelihood.
 - It does not change its arg max, but transforms a product into a sum.

$$\hat{\theta}_{\text{MLE}} = \arg \max_{\theta} \sum_{i=1}^m \log p(x^{(i)} | \theta)$$



Negative Log-Likelihood

- ▶ **Likelihood:** $L(\theta | X) = \prod_{i=1}^m p(x^{(i)} | \theta)$
- ▶ **Log-Likelihood:** $\log L(\theta | X) = \log \prod_{i=1}^m p(x^{(i)} | \theta) = \sum_{i=1}^m \log p(x^{(i)} | \theta)$
- ▶ **Negative Log-Likelihood:** $-\log L(\theta | X) = -\sum_{i=1}^m \log p(x^{(i)} | \theta)$
- ▶ Negative log-likelihood is also called the **cross-entropy**



Cross-Entropy

- ▶ **Cross-entropy**: quantify the **difference (error)** between **two probability distributions**.
- ▶ **How close** is the **predicted distribution** to the **true distribution**?

$$H(p, q) = - \sum_x p(x) \log(q(x))$$

- ▶ Where **p** is the **true distribution**, and **q** the **predicted distribution**.



Cross-Entropy - Example

- ▶ Six tosses of a coin: $X : \{h, t, t, t, h, t\}$
- ▶ The true distribution p : $p(h) = \frac{2}{6}$ and $p(t) = \frac{4}{6}$
- ▶ The predicted distribution q : h with probability of θ , and t with probability $(1 - \theta)$.
- ▶ Cross entropy: $H(p, q) = -\sum_x p(x)\log(q(x))$
 $= -p(h)\log(q(h)) - p(t)\log(q(t)) = -\frac{2}{6}\log(\theta) - \frac{4}{6}\log(1 - \theta)$
- ▶ Likelihood: $\theta^2(1 - \theta)^4$
- ▶ Negative log likelihood: $-\log(\theta^2(1 - \theta)^4) = -2\log(\theta) - 4\log(1 - \theta)$

Summary



Summary

- ▶ Logic-based AI, Machine Learning, Deep Learning
- ▶ Deep Learning models
 - Deep Feed Forward
 - Convolutional Neural Network (CNN)
 - Recurrent Neural Network (RNN)
 - Transformer
- ▶ Linear algebra and probability
 - Random variables
 - Probability distribution
 - Likelihood
 - Negative log-likelihood and cross-entropy



References

- ▶ Ian Goodfellow et al., Deep Learning (Ch. 1, 2, 3)

Questions?

Acknowledgements

Some of the pictures were copied from the book Hands-On Machine Learning with Scikit-Learn and TensorFlow, Aurelien Geron, O'Reilly Media, 2017.