## RNNs and Transformers

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## Let's Start With An Example

## Google

their work
their books
their teachers
Feeling Lucky
their homework
their lecturer their new lecturer

- Language modeling is the task of predicting what word comes next.



## Language Modeling (2/2)

- More formally: given a sequence of words $\mathrm{x}^{(1)}, \mathrm{x}^{(2)}, \cdots, \mathrm{x}^{(\mathrm{t})}$, compute the probability distribution of the next word $\mathrm{x}^{(\mathrm{t}+1)}$ :

$$
\mathrm{p}\left(\mathrm{x}^{(\mathrm{t}+1)}=\mathrm{w}_{\mathrm{j}} \mid \mathrm{x}^{(\mathrm{t})}, \cdots \mathrm{x}^{(1)}\right)
$$

- $\mathrm{w}_{\mathrm{j}}$ is a word in vocabulary $\mathrm{V}=\left\{\mathrm{w}_{1}, \cdots, \mathrm{w}_{\mathrm{v}}\right\}$.

- the students opened their
- How to learn a Language Model?
- Learn a n-gram Language Model!
- A $n$-gram is a chunk of $n$ consecutive words.
- Unigrams: "the", "students", "opened", "their"
- Bigrams: "the students", "students opened", "opened their"
- Trigrams: "the students opened", "students opened their"
- 4-grams: "the students opened their"
- Collect statistics about how frequent different n-grams are, and use these to predict next word.


## n-gram Language Models - Example

- Suppose we are learning a 4-gram Language Model.
- $\mathrm{x}^{(\mathrm{t}+1)}$ depends only on the preceding 3 words $\left\{\mathrm{x}^{(\mathrm{t})}, \mathrm{x}^{(\mathrm{t}-1)}, \mathrm{x}^{(\mathrm{t}-2)}\right\}$.
discard
condition on this

$$
\mathrm{p}\left(\mathrm{w}_{\mathrm{j}} \mid \text { students opened their }\right)=\frac{\text { students opened their } \mathrm{w}_{\mathrm{j}}}{\text { students opened their }}
$$

- In the corpus:
- "students opened their" occurred 1000 times
- "students opened their books occurred 400 times: $\mathrm{p}($ books $\mid$ students opened their $)=0.4$
- "students opened their exams occurred 100 times: $\mathrm{p}($ exams $\mid$ students opened their $)=0.1$


## Problems with n-gram Language Models - Sparsity

$$
\mathrm{p}\left(\mathrm{w}_{\mathrm{j}} \mid \text { students opened their }\right)=\frac{\text { students opened their } \mathrm{w}_{\mathrm{j}}}{\text { students opened their }}
$$

- What if "students opened their $\mathrm{w}_{\mathrm{j}}$ " never occurred in data? Then $\mathrm{w}_{\mathrm{j}}$ has probability 0 !
- What if "students opened their" never occurred in data? Then we can't calculate probability for any $\mathrm{w}_{\mathrm{j}}$ !
- Increasing n makes sparsity problems worse.
- Typically we can't have $n$ bigger than 5 .


## Problems with n-gram Language Models - Storage

$$
\mathrm{p}\left(\mathrm{w}_{\mathrm{j}} \mid \text { students opened their }\right)=\frac{\text { students opened their } \mathrm{w}_{\mathrm{j}}}{\text { students opened their }}
$$

- For "students opened their $\mathrm{w}_{\mathrm{j}}$ ", we need to store count for all possible 4-grams.
- The model size is in the order of $0(\exp (\mathrm{n}))$.
- Increasing n makes model size huge.


## Can We Build a Neural Language Model? (1/3)

- Recall the Language Modeling task:
- Input: sequence of words $x^{(1)}, x^{(2)}, \cdots, x^{(t)}$
- Output: probability dist of the next word $p\left(x^{(t+1)}=w_{j} \mid x^{(t)}, \cdots, x^{(1)}\right)$
- One-Hot encoding
- Represent a categorical variable as a binary vector.
- All recodes are zero, except the index of the integer, which is one.
- Each embedded word $\mathbf{e}^{(\mathrm{t})}=\mathbf{E}^{\top} \mathbf{x}^{(\mathrm{t})}$ is a one-hot vector of size vocabulary size.



## Can We Build a Neural Language Model? (2/3)

- A MLP model
- Input: words $\mathrm{X}^{(1)}, \mathrm{x}^{(2)}, \mathrm{x}^{(3)}, \mathrm{x}^{(4)}$
- Input layer: one-hot vectors $\mathbf{e}^{(1)}, \mathbf{e}^{(2)}, \mathbf{e}^{(3)}, \mathbf{e}^{(4)}$
- Hidden layer: $\mathbf{h}=f\left(\mathbf{w}^{\top} \mathbf{e}\right), f$ is an activation function.
- Output: $\hat{\mathbf{y}}=\operatorname{sof} \operatorname{tmax}\left(\mathbf{v}^{\top} \mathbf{h}\right)$



## Can We Build a Neural Language Model? (3/3)

- Improvements over n-gram LM:
- No sparsity problem
- Model size is $O(n)$ not $O(\exp (n))$
- Remaining problems:
- It is fixed 4 in our example, which is small
- We need a neural architecture that can process any length input



## Recurrent Neural Networks (RNN)

## Recurrent Neural Networks (1/4)

- The idea behind Recurrent neural networks (RNN) is to make use of sequential data.
- Until here, we assume that all inputs (and outputs) are independent of each other.
- Independent input (output) is a bad idea for many tasks, e.g., predicting the next word in a sentence (it's better to know which words came before it).
- They can analyze time series data and predict the future.
- They can work on sequences of arbitrary lengths, rather than on fixed-sized inputs.


## Recurrent Neural Networks (2/4)

- Neurons in an RNN have connections pointing backward.
- RNNs have memory, which captures information about what has been calculated so far.



## Recurrent Neural Networks (3/4)

- Unfolding the network: represent a network against the time axis.
- We write out the network for the complete sequence.
- For example, if the sequence we care about is a sentence of three words, the network would be unfolded into a 3-layer neural network.
- One layer for each word.



## Recurrent Neural Networks (4/4)

- $h^{(t)}=f\left(\mathbf{u}^{\top} \mathbf{x}^{(t)}+\mathrm{wh}^{(t-1)}\right)$, where f is an activation function, e.g., tanh or ReLU.
- $\hat{\mathrm{y}}^{(\mathrm{t})}=\mathrm{g}\left(\mathrm{vh}^{(\mathrm{t})}\right)$, where g can be the softmax function.
- cost $\left(\mathrm{y}^{(\mathrm{t})}, \hat{\mathrm{y}}^{(\mathrm{t})}\right)=$ cross_entropy $\left(\mathrm{y}^{(\mathrm{t})}, \hat{\mathrm{y}}^{(\mathrm{t})}\right)=-\sum \mathrm{y}^{(\mathrm{t})} \log \hat{\mathrm{y}}^{(\mathrm{t})}$
- $\mathrm{y}^{(\mathrm{t})}$ is the correct word at time step t , and $\hat{\mathrm{y}}^{(\mathrm{t})}$ is the prediction.



## Recurrent Neurons - Weights (1/4)

- Each recurrent neuron has three sets of weights: $\mathbf{u}, \mathrm{w}$, and v .



## Recurrent Neurons - Weights (2/4)

- $\mathbf{u}$ : the weights for the inputs $\mathbf{x}^{(\mathrm{t})}$.
- $\mathbf{x}^{(\mathrm{t})}$ : is the input at time step t .
- For example, $\mathbf{x}^{(1)}$ could be a one-hot vector corresponding to the first word of a sentence.



## Recurrent Neurons - Weights (3/4)

- w : the weights for the hidden state of the previous time step $\mathrm{h}^{(\mathrm{t}-1)}$.
- $\mathrm{h}^{(\mathrm{t})}$ : is the hidden state (memory) at time step t .
- $\mathrm{h}^{(\mathrm{t})}=\tanh \left(\mathbf{u}^{\top} \mathbf{x}^{(\mathrm{t})}+\mathrm{wh}^{(\mathrm{t}-1)}\right)$
- $h^{(0)}$ is the initial hidden state.



## Recurrent Neurons - Weights (4/4)

- v : the weights for the hidden state of the current time step $\mathrm{h}^{(\mathrm{t})}$.
- $\hat{\mathbf{y}}^{(\mathrm{t})}$ is the output at step t .
- $\hat{\mathbf{y}}^{(\mathrm{t})}=\operatorname{softmax}\left(\mathrm{vh}^{(\mathrm{t})}\right)$
- For example, if we wanted to predict the next word in a sentence, it would be a vector of probabilities across our vocabulary.



## Layers of Recurrent Neurons

- At each time step $t$, every neuron of a layer receives both the input vector $\mathbf{x}^{(t)}$ and the output vector from the previous time step $\mathbf{h}^{(t-1)}$.

$$
\begin{gathered}
\mathbf{h}^{(\mathrm{t})}=\tanh \left(\mathbf{u}^{\top} \mathbf{x}^{(\mathrm{t})}+\mathbf{w}^{\top} \mathbf{h}^{(\mathrm{t}-1)}\right) \\
\mathbf{y}^{(\mathrm{t})}=\operatorname{sigmoid}\left(\mathbf{v}^{\top} \mathbf{h}^{(\mathrm{t})}\right)
\end{gathered}
$$




## Deep RNN

- Stacking multiple layers of cells gives you a deep RNN.



## Let's Back to Language Model Example

## A RNN Neural Language Model (1/2)

- The input $\mathbf{x}$ will be a sequence of words (each $\mathrm{x}^{(\mathrm{t})}$ is a single word).
- Each embedded word $\mathbf{e}^{(\mathrm{t})}=\mathbf{E}^{\top} \mathbf{x}^{(\mathrm{t})}$ is a one-hot vector of size vocabulary size.



## A RNN Neural Language Model (2/2)

- Let's recap the equations for the RNN:
- $\mathrm{h}^{(\mathrm{t})}=\tanh \left(\mathbf{u}^{\mathrm{T}} \mathbf{e}^{(\mathrm{t})}+\mathrm{wh}^{(\mathrm{t}-1)}\right)$
- $\hat{\mathbf{y}}^{(t)}=\operatorname{softmax}\left(\mathrm{vh}^{(\mathrm{t})}\right)$
- The output $\hat{\mathbf{y}}^{(\mathrm{t})}$ is a vector of vocabulary size elements.
- Each element of $\hat{\mathbf{y}}^{(\mathrm{t})}$ represents the probability of that word being the next word in the sentence.



## SORBMFOB THELOMA POST CHETES A POTATO

## RNN Design Patterns

## RNN Design Patterns - Sequence-to-Vector

- Sequence-to-vector network: takes a sequence of inputs, and ignore all outputs except for the last one.
- E.g., you could feed the network a sequence of words corresponding to a movie review, and the network would output a sentiment score.

Ignored outputs


## RNN Design Patterns - Vector-to-Sequence

- Vector-to-sequence network: takes a single input at the first time step, and let it output a sequence.
- E.g., the input could be an image, and the output could be a caption for that image.



## RNN Design Patterns - Sequence-to-Sequence

- Sequence-to-sequence network: takes a sequence of inputs and produce a sequence of outputs.
- Useful for predicting time series such as stock prices: you feed it the prices over the last N days, and it must output the prices shifted by one day into the future.
- Here, both input sequences and output sequences have the same length.



## RNN Design Patterns - Encoder-Decoder

- Encoder-decoder network: a sequence-to-vector network (encoder), followed by a vector-to-sequence network (decoder).
- E.g., translating a sentence from one language to another.
- You would feed the network a sentence in one language, the encoder would convert this sentence into a single vector representation, and then the decoder would decode this vector into a sentence in another language.



## RNN in TensorFlow

## RNN in TensorFlow $(1 / 5)$

- Forecasting a time series
- E.g., a dataset of 10000 time series, each of them 50 time steps long.
- The goal here is to forecast the value at the next time step (represented by the X ) for each of them.

- Use fully connected network

```
model = keras.models.Sequential([
    keras.layers.Flatten(input_shape=[50, 1]),
    keras.layers.Dense(1)
])
model.compile(loss="mse", optimizer="adam")
history = model.fit(X_train, y_train, epochs=20)
model.evaluate(X_test, y_test, verbose=0)
# loss: 0.003993967570985357
```


## RNN in TensorFlow (3/5)

- Simple RNN

```
model = keras.models.Sequential([
    keras.layers.SimpleRNN(1, input_shape=[None, 1])
])
model.compile(loss="mse", optimizer='adam')
history = model.fit(X_train, y_train, epochs=20)
model.evaluate(X_test, y_test, verbose=0)
# loss: 0.011026302369932333
```


## RNN in TensorFlow (4/5)

- Deep RNN

```
model = keras.models.Sequential([
    keras.layers.SimpleRNN(20, return_sequences=True, input_shape=[None, 1]),
    keras.layers.SimpleRNN(20, return_sequences=True),
    keras.layers.SimpleRNN(1)
])
model.compile(loss="mse", optimizer="adam")
history = model.fit(X_train, y_train, epochs=20)
model.evaluate(X_test, y_test, verbose=0)
# loss: 0.003197280486735205
```


## RNN in TensorFlow (5/5)

- Deep RNN (second implementation)
- Make the second layer return only the last output (no return_sequences)

```
model = keras.models.Sequential([
    keras.layers.SimpleRNN(20, return_sequences=True, input_shape=[None, 1]),
    keras.layers.SimpleRNN(20),
    keras.layers.Dense(1)
])
model.compile(loss="mse", optimizer="adam")
history = model.fit(X_train, y_train, epochs=20)
model.evaluate(X_test, y_test, verbose=0)
# loss: 0.002757748544837038
```


## Training RNNs

- To train an RNN, we should unroll it through time and then simply use regular backpropagation.
- This strategy is called backpropagation through time (BPTT).


## Backpropagation Through Time (1/3)

- To train the model using BPTT, we go through the following steps:
- 1. Forward pass through the unrolled network (represented by the dashed arrows).
- 2. The cost function is $C\left(\hat{\mathbf{y}}^{\mathrm{tmin}}, \hat{\mathbf{y}}^{\mathrm{tmin}+1}, \cdots, \hat{\mathbf{y}}^{\mathrm{tmax}}\right)$, where tmin and tmax are the first and last output time steps, not counting the ignored outputs.



## Backpropagation Through Time (2/3)

- 3. Propagate backward the gradients of that cost function through the unrolled network (represented by the solid arrows).
- 4. The model parameters are updated using the gradients computed during BPTT.



## Backpropagation Through Time (3/3)

- The gradients flow backward through all the outputs used by the cost function, not just through the final output.
- For example, in the following figure:
- The cost function is computed using the last three outputs, $\hat{\mathbf{y}}^{(2)}, \hat{\mathbf{y}}^{(3)}$, and $\hat{\mathbf{y}}^{(4)}$.
- Gradients flow through these three outputs, but not through $\hat{\mathbf{y}}^{(0)}$ and $\hat{\mathbf{y}}^{(1)}$.




$\mathrm{X}_{3}$
$\mathbf{x}_{\tau}$

KTH雨 54x)

BPTT Step by Step (5/20)


BPTT Step by Step (6/20)

$\mathbf{x}_{3}$
$\mathbf{X}_{\tau}$

KTH雨 4.

BPTT Step by Step (7/20)

$\mathbf{x}_{\tau}$

BPTT Step by Step (8/20)

$\mathbf{X}_{\tau}$

BPTT Step by Step (9/20)

$\mathbf{x}_{\tau}$

BPTT Step by Step (10/20)


BPTT Step by Step (11/20)


## BPTT Step by Step (12/20)

$$
\begin{gathered}
\mathbf{s}^{(\mathrm{t})}=\mathbf{u}^{\mathrm{T}} \mathbf{x}^{(\mathrm{t})}+\mathrm{wh}^{(\mathrm{t}-1)} \\
\mathrm{h}^{(\mathrm{t})}=\tanh \left(\mathbf{s}^{(\mathrm{t})}\right) \\
\mathrm{z}^{(\mathrm{t})}=\operatorname{vh}^{(\mathrm{t})} \\
\hat{\mathrm{y}}^{(\mathrm{t})}=\operatorname{sof} \operatorname{tmax}\left(\mathrm{z}^{(\mathrm{t})}\right) \\
\mathrm{J}^{(\mathrm{t})}=\text { cross_entropy }\left(\mathrm{y}^{(\mathrm{t})}, \hat{\mathrm{y}}^{(\mathrm{t})}\right)=-\sum \mathrm{y}^{(\mathrm{t})} \log \hat{\mathrm{y}}^{(\mathrm{t})} \\
\underbrace{\hat{y}_{1}}_{U}
\end{gathered}
$$

## BPTT Step by Step (13/20)

$$
\mathrm{J}^{(\mathrm{t})}=\text { cross_entropy }\left(\mathrm{y}^{(\mathrm{t})}, \hat{\mathrm{y}}^{(\mathrm{t})}\right)=-\sum \mathrm{y}^{(\mathrm{t})} \log \hat{\mathrm{y}}^{(\mathrm{t})}
$$

- We treat the full sequence as one training example.
- The total error E is just the sum of the errors at each time step.
- E.g., $E=J^{(1)}+J^{(2)}+\cdots+J^{(t)}$



## BPTT Step by Step (14/20)

- $\mathrm{J}^{(\mathrm{t})}$ is the total cost, so we can say that a 1-unit increase in v , w or u will impact each of $\mathrm{J}^{(1)}, \mathrm{J}^{(2)}$, until $\mathrm{J}^{(t)}$ individually.
- The gradient is equal to the sum of the respective gradients at each time step $t$.
- For example if $\mathrm{t}=3$ we have: $\mathrm{E}=\mathrm{J}^{(1)}+\mathrm{J}^{(2)}+\mathrm{J}^{(3)}$

$$
\begin{aligned}
& \frac{\partial \mathrm{E}}{\partial \mathrm{v}}=\sum_{\mathrm{t}} \frac{\partial \mathrm{~J}^{(t)}}{\partial \mathrm{v}}=\frac{\partial \mathrm{J}^{(3)}}{\partial \mathrm{v}}+\frac{\partial \mathrm{J}^{(2)}}{\partial \mathrm{v}}+\frac{\partial \mathrm{J}^{(1)}}{\partial \mathrm{v}} \\
& \frac{\partial \mathrm{E}}{\partial \mathrm{w}}=\sum_{\mathrm{t}} \frac{\partial \mathrm{~J}^{(t)}}{\partial \mathrm{w}}=\frac{\partial \mathrm{J}^{(3)}}{\partial \mathrm{w}}+\frac{\partial \mathrm{J}^{(2)}}{\partial \mathrm{w}}+\frac{\partial \mathrm{J}^{(1)}}{\partial \mathrm{w}} \\
& \frac{\partial \mathrm{E}}{\partial \mathrm{u}}=\sum_{\mathrm{t}} \frac{\partial \mathrm{~J}^{(3)}}{\partial \mathrm{u}}=\frac{\partial J^{(3)}}{\partial \mathrm{u}}+\frac{\partial \mathrm{J}^{(2)}}{\partial \mathrm{u}}+\frac{\partial J^{(1)}}{\partial u}
\end{aligned}
$$

## BPTT Step by Step (15/20)

- Let's start with $\frac{\partial \mathrm{E}}{\partial \mathrm{v}}$.
- A change in $v$ will only impact $J^{(3)}$ at time $t=3$, because it plays no role in computing the value of anything other than $z^{(3)}$.

$$
\begin{aligned}
& \frac{\partial \mathrm{E}}{\partial \mathrm{v}}=\sum_{\mathrm{t}} \frac{\partial \mathrm{~J}^{(\mathrm{t})}}{\partial \mathrm{v}}=\frac{\partial \mathrm{J}^{(3)}}{\partial \mathrm{v}}+\frac{\partial \mathrm{J}^{(2)}}{\partial \mathrm{v}}+\frac{\partial \mathrm{J}^{(1)}}{\partial \mathrm{v}} \\
& \frac{\partial \mathrm{~J}^{(3)}}{\partial \mathrm{v}}=\frac{\partial \mathrm{J}^{(3)}}{\partial \hat{\mathrm{y}}^{(3)}} \frac{\partial \hat{\mathrm{y}}^{(3)}}{\partial \mathbf{z}^{(3)}} \frac{\partial \mathbf{z}^{(3)}}{\partial \mathrm{v}} \\
& \frac{\partial \mathrm{~J}^{(2)}}{\partial \mathrm{v}}=\frac{\partial \mathrm{J}^{(2)}}{\partial \hat{\mathrm{y}}^{(2)}} \frac{\partial \hat{\mathrm{y}}^{(2)}}{\partial \mathbf{z}^{(2)}} \frac{\partial \mathbf{z}^{(2)}}{\partial \mathrm{v}} \\
& \frac{\partial \mathrm{~J}^{(1)}}{\partial \mathrm{v}}=\frac{\partial \mathrm{J}^{(1)}}{\partial \hat{\mathrm{y}}^{(1)}} \frac{\partial \hat{\mathrm{y}}^{(1)}}{\partial \mathbf{z}^{(1)}} \frac{\partial \mathbf{z}^{(1)}}{\partial \mathrm{v}}
\end{aligned}
$$



## BPTT Step by Step (16/20)

- Let's compute the derivatives of $\frac{\partial J}{\partial \mathrm{w}}$ and $\frac{\partial J}{\partial \mathrm{u}}$, which are computed the same.
- A change in w at $\mathrm{t}=3$ will impact our cost J in 3 separate ways:

1. When computing the value of $h^{(1)}$.
2. When computing the value of $h^{(2)}$, which depends on $h^{(1)}$.
3. When computing the value of $h^{(3)}$, which depends on $h^{(2)}$, which depends on $h^{(1)}$.


## BPTT Step by Step $(17 / 20)$

- we compute our individual gradients as:

$$
\begin{aligned}
& \sum_{t} \frac{\partial J^{(t)}}{\partial \mathrm{w}}=\frac{\partial \mathrm{J}^{(3)}}{\partial \mathrm{w}}+\frac{\partial \mathrm{J}^{(2)}}{\partial \mathrm{w}}+\frac{\partial \mathrm{J}^{(1)}}{\partial \mathrm{w}} \\
& \frac{\partial \mathrm{~J}^{(1)}}{\partial \mathrm{w}}=\frac{\partial \mathrm{J}^{(1)}}{\partial \hat{\mathbf{y}}^{(1)}} \frac{\partial \hat{\mathbf{y}}^{(1)}}{\partial \mathbf{z}^{(1)}} \frac{\partial \mathbf{z}^{(1)}}{\partial \mathbf{h}^{(1)}} \frac{\partial \mathbf{h}^{(1)}}{\partial \mathbf{s}^{(1)}} \frac{\partial \mathbf{s}^{(1)}}{\partial \mathrm{w}}
\end{aligned}
$$



## BPTT Step by Step $(18 / 20)$

- we compute our individual gradients as:

$$
\begin{aligned}
& \sum_{\mathrm{t}} \frac{\partial \mathrm{~J}^{(\mathrm{t})}}{\partial \mathrm{w}}=\frac{\partial \mathrm{J}^{(3)}}{\partial \mathrm{w}}+\frac{\partial \mathrm{J}^{(2)}}{\partial \mathrm{w}}+\frac{\partial \mathrm{J}^{(1)}}{\partial \mathrm{w}} \\
& \frac{\partial \mathrm{~J}^{(2)}}{\partial \mathrm{w}}=\frac{\partial \mathrm{J}^{(2)}}{\partial \hat{\mathrm{y}}^{(2)}} \frac{\partial \hat{\mathrm{y}}^{(2)}}{\partial \mathbf{z}^{(2)}} \frac{\partial \mathbf{z}^{(2)}}{\partial \mathrm{h}^{(2)}} \frac{\partial \mathrm{h}^{(2)}}{\partial \mathbf{s}^{(2)}} \frac{\partial \mathbf{s}^{(2)}}{\partial \mathrm{w}}+ \\
& \frac{\partial \mathrm{J}^{(2)}}{\partial \hat{\mathrm{y}}^{(2)}} \frac{\partial \hat{\mathrm{y}}^{(2)}}{\partial \mathbf{z}^{(2)}} \frac{\partial \mathbf{z}^{(2)}}{\partial \mathrm{h}^{(2)}} \frac{\partial \mathbf{h}^{(2)}}{\partial \mathbf{s}^{(2)}} \frac{\partial \mathbf{s}^{(2)}}{\partial \mathrm{h}^{(1)}} \frac{\partial \mathrm{h}^{(1)}}{\partial \mathbf{s}^{(1)}} \frac{\partial \mathbf{s}^{(1)}}{\partial \mathrm{w}}
\end{aligned}
$$



## BPTT Step by Step (19/20)

- we compute our individual gradients as:

$$
\begin{aligned}
& \sum_{\mathrm{t}} \frac{\partial \mathrm{~J}^{(\mathrm{t})}}{\partial \mathrm{w}}=\frac{\partial \mathrm{J}^{(3)}}{\partial \mathrm{w}}+\frac{\partial \mathrm{J}^{(2)}}{\partial \mathrm{w}}+\frac{\partial \mathrm{J}^{(1)}}{\partial \mathrm{w}} \\
& \frac{\partial \mathrm{~J}^{(3)}}{\partial \mathrm{w}}= \\
& =\frac{\partial \mathrm{J}^{(3)}}{\partial \hat{\mathbf{y}}^{(3)}} \frac{\partial \hat{\mathrm{y}}^{(3)}}{\partial \mathbf{z}^{(3)}} \frac{\partial \mathbf{z}^{(3)}}{\partial \mathbf{h}^{(3)}} \frac{\partial \mathrm{h}^{(3)}}{\partial \mathbf{s}^{(3)}} \frac{\partial \mathbf{s}^{(3)}}{\partial \mathrm{w}}+ \\
& \quad \frac{\partial \mathrm{J}^{(3)}}{\partial \hat{\mathbf{y}}^{(3)}} \frac{\partial \hat{\mathrm{y}}^{(3)}}{\partial \mathbf{z}^{(3)}} \frac{\partial \mathbf{z}^{(3)}}{\partial \mathbf{h}^{(3)}} \frac{\partial \mathbf{h}^{(3)}}{\partial \mathbf{s}^{(3)}} \frac{\partial \mathbf{s}^{(3)}}{\partial \mathbf{h}^{(2)}} \frac{\partial \mathbf{h}^{(2)}}{\partial \mathbf{s}^{(2)}} \frac{\partial \mathbf{s}^{(2)}}{\partial \mathrm{w}}+ \\
& \\
& \frac{\partial \mathrm{J}^{(3)}}{\partial \hat{\mathbf{y}}^{(3)}} \frac{\partial \hat{\mathrm{y}}^{(3)}}{\partial \mathbf{z}^{(3)}} \frac{\partial \mathbf{z}^{(3)}}{\partial \mathbf{h}^{(3)}} \frac{\partial \mathbf{h}^{(3)}}{\partial \mathbf{s}^{(3)}} \frac{\partial \mathbf{s}^{(3)}}{\partial \mathbf{h}^{(2)}} \frac{\partial \mathbf{h}^{(2)}}{\partial \mathbf{s}^{(2)}} \frac{\partial \mathbf{s}^{(2)}}{\partial \mathbf{h}^{(1)}} \frac{\partial \mathbf{h}^{(1)}}{\partial \mathbf{s}^{(1)}} \frac{\partial \mathbf{s}^{(1)}}{\partial \mathrm{w}}
\end{aligned}
$$



- More generally, a change in w will impact our cost $\mathrm{J}^{(\mathrm{t})}$ on t separate occasions.

$$
\frac{\partial \mathrm{J}^{(\mathrm{t})}}{\partial \mathrm{w}}=\sum_{k=1}^{t} \frac{\partial \mathrm{~J}^{(\mathrm{t})}}{\partial \hat{\mathbf{y}}^{(\mathrm{t})}} \frac{\partial \hat{\mathrm{y}}^{(\mathrm{t})}}{\partial \mathbf{z}^{(\mathrm{t})}} \frac{\partial \hat{\mathbf{z}}^{(\mathrm{t})}}{\partial \mathrm{h}^{(\mathrm{t})}}\left(\prod_{j=\mathrm{k}+1}^{\mathrm{t}} \frac{\partial \mathrm{~h}^{(j)}}{\partial \mathbf{s}^{(j)}} \frac{\partial \mathbf{s}^{(j)}}{\partial \mathrm{h}^{(j-1)}}\right) \frac{\partial \mathrm{h}^{(\mathrm{k})}}{\partial \mathbf{s}^{(\mathrm{k})}} \frac{\partial \mathbf{s}^{(\mathrm{k})}}{\partial \mathrm{w}}
$$



## RNN Problems

- Sometimes we only need to look at recent information to perform the present task.
- E.g., predicting the next word based on the previous ones.
- In such cases, where the gap between the relevant information and the place that it's needed is small, RNNs can learn to use the past information.
- But, as that gap grows, RNNs become unable to learn to connect the information.
- RNNs may suffer from the vanishing/exploding gradients problem.


## RNN References

- Ian Goodfellow et al., Deep Learning (Ch. 10)
- Aurélien Géron, Hands-On Machine Learning (Ch. 15)
- Understanding LSTM Networks http://colah.github.io/posts/2015-08-Understanding-LSTMs
- CS224d: Deep Learning for Natural Language Processing http://cs224d.stanford.edu


## Word Embeddings

Problem: Word embeddings are context-free

| a | nice | walk | by | the | river | bank |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\left[\begin{array}{c}0.02 \\ \vdots \\ 0.02\end{array}\right]$ | $\left[\begin{array}{c}0.03 \\ \vdots \\ -0.02\end{array}\right]$ | $\left[\begin{array}{c}0.02 \\ \vdots \\ -0.07\end{array}\right]$ | $\left[\begin{array}{c}-0.08 \\ \vdots \\ 0.03\end{array}\right]$ | $\left[\begin{array}{c}-0.04 \\ \vdots \\ -0.03\end{array}\right]$ | $\left[\begin{array}{c}-0.01 \\ \vdots \\ -0.04\end{array}\right]$ | $\left[\begin{array}{c}-0.02 \\ \vdots \\ -0.03\end{array}\right]$ |


| walk |
| :--- | to the bank and get cash

$\left[\begin{array}{c}0.02 \\
\vdots \\
-0.07\end{array}\right]\left[\begin{array}{c}0.01 \\
\vdots \\
0.02\end{array}\right]\left[\begin{array}{c}-0.04 \\
\vdots \\
-0.03\end{array}\right]\left[\begin{array}{c}-0.02 \\
\vdots \\
-0.03\end{array}\right]\left[\begin{array}{c}-0.02 \\
\vdots \\
0.02\end{array}\right]\left[\begin{array}{c}-0.06 \\
\vdots \\
0.04\end{array}\right]\left[\begin{array}{c}0.01 \\
\vdots \\
-0.01\end{array}\right]$
[Peltarion, 2020]

## Word Embeddings

Problem: Word embeddings are context-free

| a | nice | walk | by | the | river | bank | walk | to | the | bank | and | get | cash |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| [0.02] | $[0.03]$ | [0.02] | -0.00] | -0.04] | -0.01] | -0.02] | $0.02]$ | [0.01] | -0.04] | -0.02] | -0.02] | [-0.06] | [0.01] |
| $\vdots$ | $\therefore$ |  | : | : | : |  |  | : | $\vdots$ |  | . | : | $\vdots$ |
| 0.02 | -0.02 | -0.07 | 0.03 | -0.03 | -0.04 | -0.03 | -0.07 | 0.02 | -0.03 | -0.03 | 0.02 | 0.04 | -0.01 |

## Word Embeddings

Problem: Word embeddings are context-free
Solution: Create contextualized representation


## From RNNs to Transformers

## Problems with RNNs - Motivation for Transformers

- Sequential computations prevents parallelization
- Despite GRUs and LSTMs, RNNs still need attention mechanisms to deal with long range dependencies
- Attention gives us access to any state...Maybe we don't need the costly recursion?
- Then NLP can have deep models, solves our computer vision envy!


## Attention is all you need! [Vaswani, 2017]

- Sequence-to-sequence model for Machine Translation
- Encoder-decoder architecture
- Multi-headed self-attention
- Models context and no locality bias

[Vaswani et al., 2017]


## Transformers Step-by-Step

## Understanding the Transformer: Step-by-Step



## Understanding the Transformer: Step-by-Step

No recursion, instead stacking encoder and decoder blocks

- Originally: 6 layers
- BERT base: 12 layers
- BERT large: 24 layers
- GPT2-XL: 48 layers
- GPT3: 96 layers

[Alammar, 2018]


## The Encoder and Decoder Blocks



## The Encoder Block


[Alammar, 2018]

## Attention Preliminaries

Mimics the retrieval of a value $v_{i}$ for a query $q$ based on a key $k_{i}$ in a database, but in a probabilistic fashion

Key $\longrightarrow$ Value
Query $q$


## Dot-Product Attention

- Queries, keys and values are vectors
- Output is a weighted sum of the values
- Weights are are computed as the scaled dot-product (similarity) between the query and the keys

$\operatorname{Attention}(q, K, V)=\sum_{i} \operatorname{Similarity}\left(q, k_{i}\right) \cdot v_{i}=\sum_{i} \frac{e^{q \cdot k_{i} / \sqrt{d_{k}}}}{\sum_{j} e^{q \cdot k_{j} / \sqrt{d_{k}}}} v_{i} \quad$| $\begin{array}{l}\text { Output is a } \\ \text { row-vector }\end{array}$ |
| :--- |

- Can stack multiple queries into a matrix $Q$

$$
\text { Attention }(Q, K, V)=\operatorname{softmax}\left(\frac{Q K^{\top}}{\sqrt{d_{k}}}\right)^{\top} V \quad \begin{aligned}
& \text { Output is again } \\
& \text { a matrix }
\end{aligned}
$$

- Self-attention: Let the word embeddings be the queries, keys and values, i.e. let the words select each other


## Self-Attention Mechanism



## Self-Attention Mechanism



## Self-Attention Mechanism in Matrix Notation



## Multi-Headed Self-Attention

## 

| ATTENTION | ATTENTION | $\ldots$ | ATTENTION |
| :---: | :---: | :---: | :---: |
| HEAD \#0 | HEAD \#1 | $\ldots$ | $Z_{7}$ |
| $Z_{0}$ | $Z_{1}$ |  | $\square$ |
| $\square$ | $\square$ | $\square$ |  |
| $\square$ | $\square$ |  |  |



## Self-Attention: Putting It All Together


[Alammar, 2018]

## Attention Visualized



## The Full Encoder Block

Encoder block consisting of:

- Multi-headed self-attention
- Feedforward NN (FC 2 layers)
- Skip connections
- Layer normalization - Similar to batch normalization but computed over features (words/tokens) for a single sample

[Alammar, 2018]


## Encoder-Decoder Architecture - Small Example


[Alammar, 2018]

## Complexity Comparison

| Layer Type | Complexity per Layer | Sequential <br> Operations | Maximum Path Length |
| :--- | :---: | :---: | :---: |
| Self-Attention | $O\left(n^{2} \cdot d\right)$ | $O(1)$ | $O(1)$ |
| Recurrent | $O\left(n \cdot d^{2}\right)$ | $O(n)$ | $O(n)$ |
| Convolutional | $O\left(k \cdot n \cdot d^{2}\right)$ | $O(1)$ | $O\left(\log _{k}(n)\right)$ |

## Results

| Model | BLEU |  |  | Training Cost (FLOPs) |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
|  | EN-DE | EN-FR |  | EN-DE | EN-FR |
| ByteNet [15] | 23.75 |  |  |  |  |
| Deep-Att + PosUnk [32] |  | 39.2 |  |  | $1.0 \cdot 10^{20}$ |
| GNMT + RL [31] | 24.6 | 39.92 |  | $2.3 \cdot 10^{19}$ | $1.4 \cdot 10^{20}$ |
| ConvS2S [8] | 25.16 | 40.46 |  | $9.6 \cdot 10^{18}$ | $1.5 \cdot 10^{20}$ |
| MoE [26] | 26.03 | 40.56 |  | $2.0 \cdot 10^{19}$ | $1.2 \cdot 10^{20}$ |
| Deep-Att + PosUnk Ensemble [32] |  | 40.4 |  |  | $8.0 \cdot 10^{20}$ |
| GNMT + RL Ensemble [31] | 26.30 | 41.16 |  | $1.8 \cdot 10^{20}$ | $1.1 \cdot 10^{21}$ |
| ConvS2S Ensemble [8] | 26.36 | $\mathbf{4 1 . 2 9}$ |  | $7.7 \cdot 10^{19}$ | $1.2 \cdot 10^{21}$ |
| Transformer (base model) | 27.3 | 38.1 |  | $\mathbf{3 . 3} \cdot \mathbf{1 0} \mathbf{1 0}^{18}$ |  |
| Transformer (big) | $\mathbf{2 8 . 4}$ | $\mathbf{4 1 . 0}$ |  | $2.3 \cdot 10^{19}$ |  |

## BERT

## BERT

Bidirectional Encoder Representations from Transformers

- Self-supervised pre-training of Transformers encoder for language understanding
- Fine-tuning for specific downstream task



## BERT Training Procedure



## BERT Training Objectives

Masked Language Modelling


Next Sentence prediction

Sentence $\mathbf{A}=$ The man went to the store.
Sentence B = He bought a gallon of milk. Label = IsNextSentence

```
Sentence A = The man went to the store.
Sentence B= Penguins are flightless.
Label = NotNextSentence
```


## BERT Fine-Tuning Examples

## Sentence <br> Classification

Question
Answering

Named Entity
Recognition


## How good are transformers?

- Scaling up models size and amount of training data helps a lot
- Best model is 10B (!!) parameters
- Two models have already surpassed human performance!!!
- Exact pre-training objective (MLM, NSP, corruption) doesn't matter too much
- SuperGLUE benchmark:

| Rank | Name | Model | URL | Score | BoolQ | CB | COPA | MultiRC | ReCoRD | RTE | Wic | wsc | AX-g | AX-b |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | ERNIE Team - Baidu | ERNIE 3.0 | [ | 90.6 | 91.0 | 98.6/99.2 | 97.4 | 88.6/63.2 | 94.7/94.2 | 92.6 | 77.4 | 97.3 | 92.7/94.7 | 68.6 |
| 2 | Zirui Wang | T5 + UDG, Single Model (Google Brain) | $\pi$ | 90.4 | 91.4 | 95.8/97.6 | 98.0 | 88.3/63.0 | 94.2/93.5 | 93.0 | 77.9 | 96.6 | 92.7/91.9 | 69.1 |
| 3 | DeBERTa Team - Microsoft | DeBERTa / TuringNLRv4 | [ | 90.3 | 90.4 | 95.7/97.6 | 98.4 | 88.2/63.7 | 94.5/94.1 | 93.2 | 77.5 | 95.9 | 93.3/93.8 | 66.7 |
| 4 | SuperGLUE Human Baselines | SuperGLUE Human Baselines | [ | 89.8 | 89.0 | 95.8/98.9 | 100.0 | 81.8/51.9 | 91.7/91.3 | 93.6 | 80.0 | 100.0 | 99.3/99.7 | 76.6 |
| 5 | T5 Team - Google | T5 | E | 89.3 | 91.2 | 93.9/96.8 | 94.8 | 88.1/63.3 | 94.1/93.4 | 92.5 | 76.9 | 93.8 | 92.7/91.9 | 65.6 |
| 6 | Huawei Noah's Ark Lab | NEZHA-Plus | - | 86.7 | 87.8 | 94.4/96.0 | 93.6 | 84.6/55.1 | 90.1/89.6 | 89.1 | 74.6 | 93.2 | 87.1/74.4 | 58.0 |

## Practical Examples

## BERT in low-latency production settings

## 6006IE Tech \arificial intellgence

## Google is improving 10 percent of searches by understanding language context

Say hello to BERT
By Dieter Bohn | @backion | Oct 25, 2019, 3:01am EDT

## Bing says it has been applying BERT since April

The natural language processing capabilities are now applied to all Bing queries globally.
George Nguyen on November 19, 2019 at 1:38 pm

## Distillation

- Modern pre-trained language models are huge and very computationally expensive
- How are these companies applying them to low-latency applications?
- Distillation!
- Train SOTA teacher model (pre-training + fine-tuning)
- Train smaller student model that mimics the teacher's output on a large dataset on unlabeled data
- Distillation works much better than pre-training + fine-tuning with smaller model

Amazon Book Reviews

## Transformers in TensorFlow using HuggingFace *

- The HuggingFace Library contains a majority of the recent pre-trained State-of-the-art NLP models, as well as over 4000 community uploaded models
- Works with both TensorFlow and PyTorch

Also check out our list of Community contributors and Organizations 9

| Search models... | Tags: All $\sim$ | Sort: Most downloads * |
| :--- | :--- | :--- |

bert-base-uncased
deepset/bert-large-uncased-whole-word-masking-squadz
distilbert-base-uncased
dccuchile/bert-base-spanish-wwm-cased *
microsoft/xprophetnet-large-wikilee-cased-xglue-ntg
deepset/roberta-base-squadz *
jplu/tf-xlm-roberta-base *
cl-tohoku/bert-base-japanese-whole-word-masking
distilroberta-base *
bert-base-cased
$\times 1 m$-roberta-base *

## Transformers in TensorFlow using HuggingFace ©

```
from transformers import BertTokenizerFast, TFBertForSequenceClassification
from datasets import load_dataset
import tensorflow as tf
dataset = load_dataset("imdb").shuffle()
tokenizer = BertTokenizerFast.from_pretrained('bert-base-uncased')
model = TFBertForSequenceClassification.from_pretrained('bert-base-uncased', num_labels=2)
train_encodings = tokenizer(dataset['train']['text'], truncation=True, padding=True)
train_dataset = tf.data.Dataset.from_tensor_slices((dict(train_encodings), dataset['train']['label']))
val_dataset = ... // Analogously
optimizer = tf.keras.optimizers.Adam(learning_rate=5e-5)
model.compile(optimizer=optimizer, loss=model.compute_loss)
model.fit(train_dataset.batch(16), epochs=3, batch_size=16)
model.evaluate(val_dataset.batch(16), verbose=0)
```


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## Wrap Up

## Summary

- Transformers have blown other architectures out of the water for NLP
- Get rid of recurrence and rely on self-attention
- NLP pre-training using Masked Language Modelling
- Most recent improvements using larger models and more data
- Distillation can make model serving and inference more tractable


